Analysis of epidemiological cohort data on smoking effects and lung cancer with a multi-stage cancer model

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A stochastic two-stage cancer model is used to analyse the relation between lung cancer and cigarette smoking. The model contains the main rate-limiting stages of carcinogenesis, which include initiation, promotion (clonal expansion of initiated cells), malignant transformation and a lag time for tumour formation. Various data sets were used to test the model. These include the data of a large prospective collaborative project carried out in 10 different European countries, the European Prospective Investigation into Cancer and Nutrition (EPIC). This new data set has not been modelled before. The model is also tested on other published data from CPS-II (Cancer Prevention Study II) of the American Cancer Society and the British doctors’ study. The analyses indicate that the EPIC data are best described with smoking dependence on the rates of malignant transformation and clonal expansion. With increasing smoking rates, saturation effects in the two exposure rate-dependent model parameters were observed. The results find confirmation in the biological literature, where both mutational effects and promotional effects of cigarette smoke are documented.

Introduction

The earliest approaches to mathematically investigate cancer began in the early 1950s. Nordling (1) and Stocks (2) proposed that several successive mutations in a cell would be necessary to explain the fact that for many carcinomas the incidence rate varies as a power of age. This has been quantitatively formulated by Armitage and Doll (3) in one of the best-known cancer models, a multi-stage model that accounts for the relation between age and cancer incidence. That was related to the number of stages needed for a normal cell to develop into a malignant cell (3). For the Armitage–Doll multi-stage model the observed number of biological stages, Armitage and Doll advanced their model into one of two stages with exponentially growing clones (4). The Armitage–Doll two-stage model has limitations in cancer risk assessment because in this model deterministic cell growth is assumed. When the growth rate is small, it is more appropriate to use a stochastic model than a deterministic one because the probability of extinction of clones, which is not considered in a deterministic model, cannot be neglected (5). This led to the development of stochastic cancer models (6–9). Stochastic cell growth of intermediate cells is assumed for the stochastic two-mutation model with clonal expansion. This two-step clonal expansion (TSCE) model is the best-known multi-step model and was developed by Moolgavkar et al. It is also known as the MVK model of Moolgavkar, Venzon and Knudson (7–9). In contrast with the Armitage–Doll model, there is a considerable amount of experimental data supporting the stochastic two-mutation model (10). A number of generalizations of the Armitage–Doll model and of the two-mutation model have been developed (10,11).

Several studies have been performed using multi-stage models to estimate cancer incidence and other biological end-points. The currently most widely used cancer models originate from the above-mentioned stochastic two-mutation model with clonal expansion (7–9). Extensive scientific investigations applied this model and its versions to study various aspects of carcinogenesis (12–15). Others have used multi-stage models and State-Vector Models to describe neoplastic transformation in vitro (16–20) and lung carcinogenesis (21). The two-stage cancer model with clonal expansion, applied in the current study, has a long history of development (15,22–28). The model simulates the main rate-limiting stages of carcinogenesis. They include a dose-dependent initiation stage (also referred to as first mutation rate), a net clonal expansion rate of initiated cells (also referred to as promotion), a second mutation rate (malignant transformation) and a lag time of tumour formation.

The present study applies this well-established stochastic cancer model with the aim to mathematically describe the effects of cigarette smoking with respect to lung cancer incidence. To achieve this goal, different data sets are used, including those of a large prospective collaborative project carried out in 10 different European countries, the European Prospective Investigation into Cancer and Nutrition (EPIC) (29). This investigation, including 519 978 individuals, is the largest ever conducted specifically on the relation between diet and cancer. The EPIC sub-data set applied in this study is new and has not been modelled before. The results of this effort are compared with the results from analysing two readily available older data sets with the aim to find a consistent mathematical description of smoking effects on lung carcinogenesis among different important data sets.

The effects of cigarette smoke are well documented in the literature. Tumour-promoting and co-carcinogenic (30–36) but
also mutagenic effects of cigarette smoke have been described (35,37–46). Tobacco smoke contains DNA-reactive carcinogens, such as nitrosamines, polycyclic aromatic hydrocarbons and pyrolysis products, such as carbolines. Enhancing and promotional factors, e.g. catechols, other phenols and terpenes, are also an important component. Cigarette smoke is a combination of genotoxic and non-genotoxic agents (47). Rubin (34) reports that the full range of experimental results favours the active participation of promoters and co-carcinogens as selective agents in addition to mutagens in the induction of lung cancer by cigarette smoking. Somatic mutations caused by cigarette smoke are very common and give rise to patches of clonally expanded epithelium harbouring one or more mutations (35). This justifies that in our model analysis cigarette smoke is allowed to influence both the mutation rates and the rate of clonal expansion. In addition to mutagenic and promotional effects, cytotoxic effects of cigarette smoke have also been reported (48–51).

Materials and methods

The two-stage model

In the two-stage model, normal stem cells (N-cells) can be transformed into cells of an intermediate form (I-cells) at a stochastic event rate μ1, often referred to as first mutation rate. These intermediate cells can divide into two intermediate cells at a stochastic rate α and die or differentiate at rate β. In addition, intermediate cells can divide into one intermediate and one malignant cell (M-cell) with a second stochastic event rate μ2. The malignant cells are assumed to develop into a tumour (T) after a deterministic lag time, hlag. A conceptual view of the two-stage model is given in Figure 1.

The mathematical and statistical properties of this stochastic cancer model have been discussed in great detail in the literature and will not be repeated here (13,15,23,26,27,52).

The parameterizations used for the two mutation rates and the clonal expansion rate allow these parameters to increase linearly at low smoking rates and to saturate at high smoking rates. A function \( f(x; p_1, p_2) \) is used that has the following form:

\[
f(x; p_1, p_2) = p_2 \left( 1 - \exp \left( -\frac{p_1}{p_2} x \right) \right),
\]

where \( p_1 \) (day per cigarette) is the slope of the linear part in \( f(x; p_1, p_2) \) and \( p_2 \) is the plateau value. The dose rate (in cigarette per day) is denoted as \( D \). The background rate of net clonal expansion is \( e_0 \) (per year). The background mutation rate of first and second mutation is denoted as \( \mu_0 \) and \( \mu_2 \). The parameters to estimate \( \mu_0 = \mu_2 = \mu_0 \) is used together with \( N = 10^7 \) of \( N = 10^7 \) cells is reached at an age of 20 years. The restriction \( \mu_0 = \mu_2 = \mu_0 \) was applied because only the product \( N \times \mu_0 \times \mu_0 \) can be identified from the data. In addition, the restriction \( \beta = 0 \) was used. The motivation for this approach in RIVM’s implementation of the stochastic two-stage model was discussed (53). Briefly, this approach avoids the levelling of the hazard at very high ages due to the stochasticity of separate birth and death processes of I-cells. At RIVM the exact analytical solution of the stochastic two-stage model (23,52) has been used for the present study with recent adaptations to the software (25). The specific details associated with the two-stage model as used at RIVM have been described earlier (22,24).

From the model solution the age-specific tumour hazard can be calculated for specific exposures. Lifetime risks are calculated from the age-integrated hazard function at an age of 75 years (H75) with and without exposure:

\[
LERR = \frac{H75(E) - H75(0)}{H75(0)},
\]

where LEAR and LERR are the lifetime excess absolute and relative risks, respectively.

Simultaneously to the RIVM model analyses, our colleagues at ISI also performed fits of the EPIC data using the well-established TSCE model (15,26,27) in the parameterization presented in ref. (13). In the ISI studies, different optimization routines were used than the ones applied at RIVM (described below).

The data

While the main part of this study is focussed on the EPIC data set, two other sets of data are also considered for a comparison of the smoking dependencies found by analysing them.

EPIC data. EPIC is a multi-centre prospective cohort study designed to investigate the relation between diet, nutritional and metabolic characteristics, various lifestyle and environmental factors and the incidence of different forms of cancer. The study is based in 23 collaborating centres in 10 European countries and includes populations characterized by large variations in dietary habits and cancer risk. Data are collected on diet, physical activity, reproductive history, lifetime consumption of alcohol and tobacco, previous and current illnesses and current medication (29). Estimations based on the incidence of specific cancer sites suggested that national studies of the order of 35,000–50,000 subjects, for a total European cohort of 400,000 subjects, would provide sufficient power to detect statistically significant relative risks as low as 1.2 for all major cancer sites in the entire cohort (29).

The questionnaires on non-diary variables contained a major core component, common to all EPIC centres, which includes detailed questions on life history of tobacco smoking, past and current illnesses and health problems (29). The 519,978 eligible study subjects were mostly aged 25–70 years. In the 1993/911 person-years of follow-up since 1992, 1074 incident lung cancers had been included in the database of the International Agency for Research on Cancer (IARC) by June 2002 (54). For various reasons (such as a history of previous cancer of another site, missing date of diagnosis of lung cancer and lack of follow-up information), some of these cases had to be excluded, which left 860 with satisfactory case data to be used in the analysis (54).

In addition to the above-mentioned exclusions performed on the original EPIC data, additional individuals were excluded when the EPIC sub-data set, which was used in the present study, was created. These were individuals who smoked pipe or cigar and those with missing or incomplete smoking information. Persons who stopped smoking and later started again and who stopped for longer than 20% of the total time between the very first start and the final stop of smoking were not included either. This exclusion was made because the timing of the non-smoking period was unknown in most countries. In addition,
any data from France were excluded because in the primary data collection in France no difference is made between primary lung cancer and metastases from primary cancers in locations other than the lung. Such a distinction can only be made after follow-up through medical records, which had not yet been completed in all cases. Table II shows the number of lung cancer cases and person-years for males and females in the EPIC sub-data set as used in the present study. For every individual the data contain information on the following aspects: smoking status (1 = never smoker, 2 = former smoker, 3 = current smoker), code for country centre, code for lung cancer (1 = lung cancer diagnosed, 2 = no cancer), age when smoking was started, age when smoking was stopped and the number of cigarettes smoked per day at the ages of 20, 30, 40 and 50 years. The data also comprise the year, month and day of birth; the year, month and day when the follow-up ended (i.e. the last day for which the data set is valid for that person); and the year, month and day that the person was included in the study. For every individual the data set also includes a mean number of cigarettes smoked per day in the past. Only individuals who did not have a lung tumour were allowed to enter the study. For those study subjects who had a lung cancer diagnosed during their follow-up time, the end date of their follow-up is identical to the date of tumour diagnosis. To facilitate extensive analyses by limiting the computer time in the model fits, the individual EPIC sub-data sets for males and females used for the current study were also lumped into grouped person-year strata. Therefore, the five categories shown in Table III were introduced. This led to 2118 groups for the EPIC data for males and 1834 groups for the females. First, the grouped data were used to test the model and to find the simplest model description. Final model fits were then performed with the individual EPIC data using the best estimates of the grouped data fits as starting signals a significant statistical improvement of a joint fit compared with the separate fits. That does not necessarily indicate that the joint fit is a worse description than the separate fits because the reduced number of free parameters associated with the joint fit has to be corrected for. A negative value for $\Delta_{cor}$ signals a significant statistical improvement of a joint fit compared with the separate fits. Although the largest uncertainty in the parameter values depends on the choices made for the functions chosen for the model parameters (see above), confidence intervals (CIs) for the parameter estimates are reported for the fitted parameters. The upper (and lower) limits for the CIs are determined by adjusting one parameter and performing a local refit of the other free parameters, until a specified increase in $-\log$-likelihood is obtained (see ref. 58 for the method). Ninety-five per cent CIs are reported for the parameters (corresponding to an increase in $-\log$-likelihood of 1.96).

Best estimates of the free model parameters are gained by minimizing the $-\log$-likelihood in a global search using the Adaptive Simulated Annealing (ASA) software (59,60), followed by two local optimization routines, Powell and Amoeba. The method of Simulated Annealing is a technique that has attracted significant attention as suitable for optimization problems of large scale, especially ones where a desired global maximum is hidden among many, poorer, local maxima. Both Amoeba and Powell are local search methods capable of finding the best local solution when approximate best parameters are already known. The Powell method (61) is a direction-set (steepest descent) method. Amoeba is a minimization routine that is based upon the Downhill Simplex Method (62).
Results

**EPIC data**

The following model parameters were estimated by data fitting: $\mu_0$, $e_0$, $y_1$, $m_1$, and $e_i$, $i = 1, 2$. Here, index $i = 1$ indicates the slope parameters and index $i = 2$ refers to the plateau parameters [see eq. (1) and Table I]. The slope parameters for first and second mutation rates and for the rate of net clonal expansion are $y_1$, $m_1$, $e_1$, respectively. The corresponding three plateau parameters are $y_2$, $m_2$, $e_2$. Starting with a linear smoking-rate dependence for $\mu_1(s)$ and $\mu_2(s)$ without any saturation effects and with a constant $e$, systematic fits of the grouped EPIC data for males and females were performed to evaluate whether adding additional free parameters out of those mentioned above, lead to a statistically significant improvement of the model fits. The likelihood ratio test was used to achieve this. The best estimate results from the model fits of the grouped data were taken as starting values for fits of the individual EPIC data for males and females using the two local search algorithms. When identical slope parameters ($y_1 = m_1 = e_1$) were used for $\mu_1(s)$, $\mu_2(s)$ and $e(s)$, the fits turned out to be equally good on statistical grounds compared with the fits that allowed for different slopes (results not shown).

The best model fits were those that allowed for saturation in $\mu_1(s)$, $\mu_2(s)$ and $e(s)$. The parameter $y_2$, however, was associated with infinitely large CIs, which indicated that the smoking dependence in $\mu_1(s)$ was highly uncertain. Follow-up fits indeed revealed that when no smoking dependence was allowed for $\mu_1$ in the fits of EPIC males and females (individual data), the increase in $-\log$likelihood was not significant for the males and borderline significant for the females. Detailed results are given in Table IV. For the lag time, $t_{lag}$, a constant of 5 years was used (24). When $t_{lag}$ was allowed to be free in the fit of EPIC males, it was found that the best estimate was very close to 5 years and the best estimates of the other free parameters were very close to those reported in Table IV.

The differences in the background parameters ($\mu_0$ and $e_0$) in columns 2 and 3 in Table IV are not very large and it cannot be said a priori whether male and female data sets together can be simulated with the same set of parameters. All joint fits were performed with identical slope parameters $e_1 = m_1$. In the joint fit-RIVM3 the number of free parameters was reduced from $2 \times 5$ to 5. When the same background parameters were used, the resulting $-\log$likelihood was 4420.56 (fit-RIVM3), which is 2.61 points larger than the $-\log$likelihoods of the separate fits (fit-RIVM1 and fit-RIVM2). Considering that at the 5% significance level a reduction by 5 free parameters corresponds to an increase of 5.54 points in $-\log$likelihood, it is evident that the joint fit of the EPIC data for males and females is preferable to the separate fits ($\Delta_{corr} = -2.93$, Table IV).

The ISI group also performed fits of the individual EPIC data using the TSCE model (15,26,27) in the parameterization presented in ref. (13). They found very similar tendencies for the smoking dependence of first and second mutation rate and of the net clonal expansion rate, $e$. Analogous to the findings at RIVM, it was found that on the basis of statistical grounds a joint fit of EPIC males and females is preferable to the separate fits (results not shown). Because of these similarities in the findings of both groups it was decided to only show the results based on the RIVM analyses. Figure 2 shows the exposure-dependence of the relative rates for the first and second mutation and the net clonal expansion for fit-RIVM3.

The agreement between data and model fits cannot be easily illustrated graphically, since the fit is based on individual information such as the age at time of inclusion and the age-dependent exposure pattern. In Figure 3, a comparison of observed and modelled lung cancer deaths is given for EPIC males and females in groups of exposure rate. The results from fit-RIVM1 and fit-RIVM2 (Table IV) are indicated with solid lines in Figure 3. The results found at ISI are very similar (not shown).

**EPIC data countrywise**

As described in the Materials and methods section, the two grouped EPIC data sets for males and females were also split by countries, and their information was grouped into $2 \times 9$ smaller data sets for the 9 different countries. No males from Norway are included in the EPIC data. The aim of this analysis is to find out whether the cancer incidence of different populations can be described using different background mutation rates and one joint set of smoking dependent parameters. Again, $\mu_1(s) = \mu_0$ was used in these analyses.

A joint fit of the grouped data for males split by countries was performed that allowed only for eight different free background mutation rates for the eight different countries. In this

### Table IV. Best estimates with 95% CIs (in parentheses) and $-\log$likelihood values for different model fits with $e_1 = m_1$

<table>
<thead>
<tr>
<th>Column</th>
<th>EPIC males, fit-RIVM1</th>
<th>EPIC females, fit-RIVM2</th>
<th>Males and females, fit-RIVM3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initiation</td>
<td>$\mu_0$ (per year)</td>
<td>$2.03 \times 10^{-7}$ ($1.36 \times 10^{-7}$–$2.60 \times 10^{-7}$)</td>
<td>$1.85 \times 10^{-7}$ ($1.36 \times 10^{-7}$–$2.47 \times 10^{-7}$)</td>
</tr>
<tr>
<td></td>
<td>$y_1$ (day per cigarette)</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td></td>
<td>$y_2$</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Promotion</td>
<td>$e_0$ (per year)</td>
<td>$6.6 \times 10^{-2}$ ($5.1 \times 10^{-2}$–$8.6 \times 10^{-2}$)</td>
<td>$6.3 \times 10^{-2}$ ($4.5 \times 10^{-2}$–$7.9 \times 10^{-2}$)</td>
</tr>
<tr>
<td></td>
<td>$e_1$ (day per cigarette)</td>
<td>$m_1$</td>
<td>$m_1$</td>
</tr>
<tr>
<td></td>
<td>$m_2$</td>
<td>$1.08$ ($0.65$–$1.63$)</td>
<td>$1.28$ ($0.82$–$2.14$)</td>
</tr>
<tr>
<td>Malignant transformation</td>
<td>$m_1$ (day per cigarette)</td>
<td>$0.16$ ($0.11$–$0.26$)</td>
<td>$0.15$ ($0.11$–$0.26$)</td>
</tr>
<tr>
<td></td>
<td>$m_2$</td>
<td>$1.78$ ($0.91$–$6.12$)</td>
<td>$1.75$ ($0.59$–$10.99$)</td>
</tr>
<tr>
<td>$-\log$likelihood</td>
<td>2213.16</td>
<td>2204.79</td>
<td>4417.96</td>
</tr>
</tbody>
</table>

In the fourth column the EPIC data for males and females were fitted simultaneously.
fit the best estimates of an earlier fit (results similar to fit-RIVM1, not shown) of the grouped data for males not split by countries were used as fixed input values. The best estimates together with their CIs are plotted in Figure 4A. It indicates that one joint background mutation rate could probably be used for all males from Greece, the Netherlands and Sweden; one for Spain, Italy, Denmark and the UK; and one separate for Germany. Fit-RIVM5 (Table V) confirmed that and therefore represents a consistent mathematical description of the males in the EPIC data when split by countries. The $C_0$ loglikelihood of fit-RIVM5 represents also a significant improvement over a fit that allowed two free $m_0$s (one for Germany and one for all other countries; results not shown). The latter fit was again a significant improvement over fit-RIVM4, which only allowed for one $m_0$ for all countries. The $-\log$likelhood values reported in Table V cannot be compared with those given in Table IV because the latter refer to the individual data sets, whereas for the grouped data the Poisson likelihood from eq. (5) was evaluated.

Similar tendencies were found for the females, where the best description allowed for a joint background mutation rate for Spain and Greece and one for all other countries (Figure 4B and Table V: fit-RIVM7). Allowing for different $m_0$s for Spain and Greece did not lead to a significant improvement (results not shown). Fit-RIVM7 represents a significant improvement over another fit that allowed for one $m_0$ for Greece and one for all other countries (results not shown), which was also a significant statistical improvement over fit-RIVM6.

**Age-dependent cumulative incidence and hazard**

Rather similar patterns were found among males and females for the cumulative incidence, the hazard rate and the excess relative hazard. It was therefore decided to show these curves based on the best estimated values of fit-RIVM3, the joint fit of EPIC males and females. Figure 5A gives the cumulative incidence (lifetime probability for lung cancer) with the best estimates taken from fit-RIVM3. The results given in this figure were calculated for hypothetical smoking histories, that is, a non-smoker, two ex-smokers and one lifelong smoker. The ex-smokers started to smoke at age 20 and stopped smoking at age 50. The smoking rates for the two ex-smokers were 10 and 20 cigarettes per day, respectively. The lifelong smoker also started at age 20 and smoked 20 cigarettes per day. The corresponding hazard rates are plotted versus age in Figure 5B. Figure 5C gives the excess relative hazard (excess relative risk), which is defined as [hazard (smoker)/hazard (non-smoker)] − 1.

In Figure 6 the lifetime excess absolute risk (LEAR) and lifetime excess relative risk (LERR) versus smoking rate are given for a lifelong male and female smoker who started...
Table V. EPIC males and females: best estimates and 95% CIs (in parentheses) for the background mutation rates are given for different model fits

<table>
<thead>
<tr>
<th></th>
<th>EPIC males</th>
<th>EPIC females</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Males</td>
<td>Females</td>
</tr>
<tr>
<td>μ₀ (10⁻⁷ per year) for all (other) countries</td>
<td>2.35 (2.28–2.43)</td>
<td>2.54 (2.45–2.63)</td>
</tr>
<tr>
<td>μ₀ (10⁻⁷ per year) for Germany</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>μ₀ (10⁻⁷ per year) for Greece, Netherlands, Sweden</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>–loglikelihood</td>
<td>617.42</td>
<td>532.59</td>
</tr>
<tr>
<td></td>
<td>Fit-RIVM4</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>2.40 (2.29–2.52)</td>
<td>2.62 (2.52–2.72)</td>
</tr>
<tr>
<td></td>
<td>fit-RIVM6</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>605.10</td>
<td>526.35</td>
</tr>
<tr>
<td></td>
<td>Fit-RIVM7</td>
<td></td>
</tr>
<tr>
<td></td>
<td>–loglikelihood</td>
<td></td>
</tr>
<tr>
<td></td>
<td>fit-RIVM9</td>
<td></td>
</tr>
<tr>
<td></td>
<td>–loglikelihood</td>
<td></td>
</tr>
</tbody>
</table>

Joint analysis with other data

In addition to the EPIC data, other sets of smoking data have also been analysed with the aim of finding a consistent description. From the analyses of the EPIC data the effect of smoking on μ₁ is indeterminable. This was an additional motivation to include other data sets with larger follow-up. At first, these additional data sets were analysed separately from the EPIC data to find the trends for μ₁, μ₂ and ε associated with these data.

CPS-II. Because of the limited number of different exposure rates in this data set, it was not possible to determine the slope parameters and the plateau values for μ₁, μ₂ and ε by fitting the model to the data. Different approaches were taken instead. In all of them the background rates, μ₀ and ε₀, were always estimated by data fitting. It was found that it is possible to determine the values of the three different plateaus (y₂, m₂ and e₂) when the value for the joint slope parameter is taken as a fixed input. In fit-RIVM8 (Table VI) the value for y₁ = m₁ = e₁ was used from a joint fit of EPIC males and females (grouped data) and values for the plateaus were determined by data fitting. To find a consistent description with the EPIC data, a series of model fits was performed that applied a constant m₁(s) = μ₀. In all of these fits the –loglikelihood was significantly elevated compared with fit-RIVM8. That points to a smoking rate-dependent first mutation rate for the CPS-II data. A sensitivity analysis was conducted with respect to the start age of smoking, which was assumed to be 18 years. Except for y₂ the best estimate values from Table VI are very insensitive to changes in the start age. The sensitivity found for y₂ can be expected on the basis of the rather large 95% CI for this free parameter as reported in Table VI.

British doctors’ data. Although the British doctors’ data comprise more different exposure rates than the CPS-II data (from 2.7 to 38 cigarettes per day there are eight different smoking rate strata versus only two in the CPS-II), it was not possible to determine all three slope parameters and the plateau parameters in one fit and with finite CIs. When fixed values for the slope parameters were used, the best estimates for the plateau parameters y₂ and m₂ were always found to be as large as allowed by the input ranges, indicating that the data are consistent with linear mutation rates over the smoking rates in the data set (Table VI: fit-RIVM9, –loglikelihood = 28.73, 18, 2011).
Another model fit applied \( m_1(s) = m_0 \) but led to a somewhat larger loglikelihood with the same number of free parameters. This suggests that the British doctors’ data are consistent with a smoking dependence in the first mutation rate.

Because of the very low value found for \( \varepsilon_2 \), the net rate of clonal expansion is nearly constant over the whole exposure range. The fitted values for \( y_2 \) and \( m_2 \) are associated with a very high degree of uncertainty (Table VI). Therefore, it is not possible to determine at which exposure rates the first and second mutation rates saturate.

5 free parameters). Another model fit applied \( \mu_1(s) = \mu_0 \) but led to a somewhat larger loglikelihood with the same number of free parameters. This suggests that the British doctors’ data are consistent with a smoking dependence in the first mutation rate.

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**EPIC data (males and females) and CPS-II data**

The grouped EPIC data for males and females and the CPS-II data were then used within joint model fits. This was done in an approach where smoking dependence was allowed in \( \mu_1 \) but also for a constant \( \mu_1 \) [i.e. \( \mu_1(s) = \mu_0 \)]. With this approach we
Table VI gives the results of a joint fit of the grouped EPIC data for males and females (fit-RIVM9): $\loglikelihood = 394.54$ and $\loglikelihood = 766.55$, respectively. The resulting loglikelihood values of a fit of the grouped EPIC males data and fit-RIVM9: $\loglikelihood = 359.77 + 28.73 = 388.5$. Considering the reduction of free parameters, fit-RIVM1 is at the $5\%$ level slightly worse than the separate fits. Another joint model fit that allowed for two different $\mu_0$s for the two sets of data only led to a small but significant improvement in $\loglikelihood$ (results not shown). A joint fit that did not allow for smoking dependence in $\mu_1$ led to a much higher value for the $-\loglikelihood$ (i.e. to a worse description than fit-RIVM1).

Figure 7 gives the risk predictions calculated with the best estimate values of the fits of EPIC males (grouped and individual data), the British doctors’ data (fit-RIVM9) and the joint fit of EPIC males and the British doctors’ data (fit-RIVM11). The curves refer to lifelong model smokers who started smoking at age 20, smoking $0–60$ cigarettes per day. The British doctors’ data comprise $8$ mean smoking rates from $2.7$ to $38$ cigarettes per day ($56$). In the EPIC study a majority of the individuals also have smoking rates in this range. The similar $-\loglikelihood$ values for the joint and the separate fits (Table VI) therefore confirm the similar risk values at low exposure rates. Figure 7 shows that the various risk predictions are similar for low smoking rates but different at higher rates. When the grouped EPIC data were fitted, the resulting best estimate values for the plateau parameters turned out to be larger compared with the results from fit-RIVM1. This is reflected in the faster saturation of the risk functions that are based on the individual fit. It should be emphasized that this fit of the grouped data allowed for a smoking dependence in $\mu_1$, whereas fit-RIVM1 did not.

### Discussion

The aim of the present analysis was to describe the smoking-related lung cancer risk in a large European epidemiological cohort data set using the stochastic two-stage model. Two other
historical data sets have also been analysed with the aim to find a consistent mathematical description with the EPIC data.

**EPIC data**

The analyses started out by using the EPIC data in a grouped form to do extensive global searches in the large parameter space. With the best estimates from these analyses as starting values, follow-up fits were then performed with the individual EPIC data. Model fits to the EPIC data for males and females revealed a smoking dependence for the second mutation rate, $\mu_2$, and the clonal expansion parameter, $\varepsilon$. A saturation behaviour for high smoking rates was also found (Figure 2). It should be emphasized that the very large CIs that were found for $\gamma_2$ in the fit, that still allowed for $\mu_1$ to be smoking dependent, do not prove the absence of smoking dependence for this rate. It merely shows that the information that is contained in the EPIC data does not allow the determination of any possible smoking dependence of $\mu_1$ with reasonable certainty.

The findings of smoking action presented here reflect those of an earlier study with the TSCE model. There, smoking had an effect on promotion and malignant transformation but not on initiation (63). Another study by Heidenreich *et al.* (64) confirmed these trends for smoking and radon-exposed rats. As it can be seen in Figure 3, the model fits the data well at low, medium and at high exposure rates.

One fit of the individual data set of EPIC males has also been performed with $\beta$ as a free parameter in addition to the other free parameters. This fit did not lead to very different results for the other free parameters. The $-\log$-likelihood was, however, significantly improved compared with fit-RIVM1 (Table IV).

Arguments for not including $\beta$ as a free parameter have been given (53).

A consistent model description for males and females was achieved by fitting the two different individual EPIC data sets for males and females jointly with one set of free parameters for males and for females. The fact that consistent descriptions of the EPIC data for males and females were found is an important result. Only one set of smoking-dependent parameters is necessary to describe these data. From the analysis of the EPIC data with the two-stage model we found no differences in the background rates and in the smoking-related parameters for males and females. In our modelling approach, all differences in lung cancer incidence between males and females can be attributed to differences in their smoking habits.

To investigate the relative importance of smoking rate, age at start of smoking and the smoking duration on the cancer risk, a series of simulations was performed using the best estimates of the joint fit of EPIC males and females (fit-RIVM3). The first simulation used a set of model smokers who all started smoking at age 20 and smoked their entire life at smoking rates of 20, 30, 40, 50 and 60 cigarettes per day. The data set also contained a non-smoker. Ratios of the excess relative risks (ERR) for various smoking rates were then calculated at an age of 70 years. Analogous simulations were also performed for a group of men and women who started at various ages and smoked 20 cigarettes per day for life. To assess the influence of smoking duration, another simulation was performed for a set

![Fig. 7. Lifetime excess absolute (A) and excess relative risk (B) versus exposure rate $s$ for lifelong smokers. Smoking was started at an age of 20 years. Three of the curves are based on best estimates given in Tables IV and VI.](image)

<table>
<thead>
<tr>
<th>Table VII. Ratios of the excess relative risk (ERR) for three different simulations of male and female model smokers</th>
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<tbody>
<tr>
<td>Start age 20, lifelong smokers</td>
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<tr>
<td>ERR ($s = 60$ cigarettes per day)/ERR ($s = 20$ cigarettes per day)</td>
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<tr>
<td>ERR ($s = 50$ cigarettes per day)/ERR ($s = 20$ cigarettes per day)</td>
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<td>ERR ($s = 40$ cigarettes per day)/ERR ($s = 20$ cigarettes per day)</td>
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<tr>
<td>ERR ($s = 30$ cigarettes per day)/ERR ($s = 20$ cigarettes per day)</td>
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<tr>
<td>$s = 20$ cigarettes per day, lifelong smokers</td>
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<tr>
<td>ERR (start age 15)/ERR (start age 55)</td>
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<td>ERR (start age 25)/ERR (start age 55)</td>
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<td>ERR (start age 35)/ERR (start age 55)</td>
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<td>ERR (start age 45)/ERR (start age 55)</td>
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<td>$s = 20$ cigarettes per day, start age 20</td>
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<td>ERR (stop age 70)/ERR (stop age 30)</td>
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<td>ERR (stop age 60)/ERR (stop age 30)</td>
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<td>ERR (stop age 50)/ERR (stop age 30)</td>
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<td>ERR (stop age 40)/ERR (stop age 30)</td>
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The best estimates of fit-RIVM3 were applied. The ERRs refer to an age of 70 years.
of model smokers who all started smoking at age 20 and who stopped at various times after smoking 20 cigarettes per day. The results are summarized in Table VII. They indicate that with respect to cancer risk it is mainly the ages (age of smoking initiation and duration of smoking) that matter and that the smoking rates make a smaller difference. The latter reflects the saturation behaviour found for μ2 and ε (refer to Figure 2). With respect to public health interventions these findings imply that teenage smoking should be prevented and that smoking should be stopped as early as possible.

The EPIC data were also analysed countrywise. We found that, if countrywise variations are allowed, it was preferable to describe the eight different data sets for males with the same set of smoking coefficients but with three different background mutation rates. Similar results were found for the females. The differences in baseline cancer incidence in different populations were described by different background mutation rates with one joint set of smoking parameters. This suggests the possibility of risk transfer between populations of different countries. Figure 4B shows the finding that the women from Greece and Spain have lower background mutation rates than the women from other countries. This corresponds to the fact that in the EPIC cohort the lung cancer incidence rate per 100,000 person-years is lowest for women from Greece and second lowest for women from Spain (Table I in ref. 54). In this comparison, however, one has to bear in mind that Miller et al. (54) give the incidence rates for the whole EPIC cohort, including smokers and ex-smokers. The differences in μ0 also reflect differences in dietary habits, environmental pollution, radon concentrations, genetic make-up and also possible differences in detection rates and diagnostic criteria for lung cancer in different EPIC study centres.

The age-specific cumulative incidence given in Figure 5A shows that quitting to smoke at a certain age (here 50 years) shows an instantaneous effect in the cumulative incidence with a time delay due to tlag of 5 years. The sudden increase in the hazard tlag after smoking was started is due to the smoking effect on μ2. The same holds for the pronounced decrease of the hazard rate tlag after smoking was stopped. After the initial sudden increase of the hazard an additional smaller increasing effect is visible in Figure 5B, reflecting the influence of ε(s). The hazard for non-smokers increases roughly exponentially (lower curve in Figure 5B) and so do the hazards for ex-smokers, with sharp decreases 5 years after smoking was stopped. In reality, tlag, the growth time from a malignant cell into a fatal tumour, would follow a distribution and that would attenuate the decrease. The hazard for ex-smokers does not reduce to the hazard of non-smokers. This has also been found by others (63,65). Similar to the findings of the most recent study on smoking-related mortality in male British doctors (66), we found that smoking cessation at an age of 50 approximately halves the hazard. The results given in Figure 5C indicate that cigarette smoking leads to a marked increase in excess relative risk. The hazard rates given in Figure 5B do not level at high ages as found by others (63,67). This has to do with the fact that β = 0 was used in the RIVM fits together with the setting μ01 = μ02. Very similar risk patterns have been found by the ISI group.

The saturation in the risk functions in Figure 6 means that there is not much difference in lung cancer risk between smokers of, for example, 40 and 50 cigarettes per day. At low smoking rates the risk predictions for males and females turn out to be rather similar, reflecting the similarities in the best estimates of the slope parameter m1 with largely overlapping 95% CIs (Table IV). Figure 6A and B shows that the predicted risks for males who smoke heavily are lower than those for females at high smoking rates. This reflects the lower best estimate value for ε1 found in fit-RIVM1 compared with fit-RIVM2 (Table IV). The risk predictions for males and females at high smoking rates are associated with some uncertainties due to the larger 95% CIs for μ2 in the associated model fits (Table IV). Again, it was found that ISI predicts similar risks at all exposure rates.

The bio-mathematical model description of smoking effects presented in this paper could also be important in analyses of the joint effects of radiation and smoking on lung cancer risk among atomic bomb survivors. A recent study on this subject points out the possibility of misleading inferences about radiation risks among A-bomb survivors when smoking effects are ignored (68).

Possible influence of first mutation rate

When μ1 = μ1(s) was allowed in the model fits of EPIC males and females, the largest smoking dependence was found in μ1 with very large CIs and a somewhat smaller influence on μ2. At higher smoking rates saturation occurs. The smallest exposure rate dependence was associated with ε, which consequently saturated fastest. As mentioned above, the large uncertainties associated with the estimated value for μ2 indicate the use of a constant μ1 = μ0. The EPIC data could, however, still be consistent with a smoking rate-dependent first mutation rate. Concerning risk estimates, any possible smoking influence on μ1 would lead to a slightly stronger increase and decrease in the hazard rate after smoking was started and stopped, respectively.

Although the follow-up time available in the EPIC study is limited (the average follow-up duration is 5 years), the data contain a reconstruction of the smoking histories of all individuals in the study. This reconstruction, however, is subject to errors and biases. That might explain the large uncertainties that were found for the plateau value γ1 of μ1 because it is the initiation part that depends on the smoking history from a longer time ago. For radiation this has been illustrated (69). They showed that an effect on initiation only appeared ~60 years after the exposure ended (see Figure 3 in ref. 69), as cells that were initiated by an exposure still need to undergo clonal expansion, malignant transformation and the lag time until they can be detected as a lung cancer. Because most person-years in the EPIC study are in the age range of 40–65 years, not many subjects are observed with smoking exposure more than 50 years ago, which might explain the large uncertainty in estimating the effects of smoking on μ1.

An interesting question to consider relates to the influence that a smoking-dependent first mutation rate would have on the risk patterns. This was investigated using the results from fit-RIVM3 (joint fit of EPIC males and females) and another analogous model fit that allowed for μ1 = μ1(s). With the best estimated values from these fits the excess relative hazards and the lifetime risks (LEAR and LERR) were calculated for different model smokers who started smoking at different ages and for different periods of time. It was found that the ratio of the excess relative hazards for model fits with and without smoking-dependent μ1 was largest for those model smokers who started smoking earlier. The ratio was highest for smokers who started smoking at young ages and who only smoked for short periods of time. For example, for individuals who
started smoking 20 cigarettes per day at an age of 15 years and who smoked for 5 years, the ratio in excess relative hazard was \( \sim 3.5 \). These findings are in accordance with the patterns detected by Luebeck and Hazelton (69) as pointed out in the previous paragraph (refer to Figure 3 in ref. 69). To find any influence that an exposure might have on initiation it is therefore advisable to include many individuals in epidemiological studies who started smoking very early in their life and who also quit smoking early.

**Discussion of joint analysis with other data**

Fitting the CPS-II data showed the strongest carcinogenic action of cigarette smoke at the first mutation rate with smaller smoking dependencies in \( \mu_2(s) \) and \( \epsilon(s) \) and saturation in all three model parameters (Table VI). Any approach that applied a constant and smoking rate-independent \( \mu_1(s) = \mu_0 \) led to strongly increased \( -\log \) likelihood values. This suggested a smoking rate-dependent first mutation rate for the CPS-II data. The analysis of the British doctors’ data showed a strong linear smoking dependence in \( \mu_1(s) \) and \( \mu_2(s) \) with almost no influence on \( \epsilon(s) \). Because of the small number of smoking rate values available in these two data sets, only limited information on the smoking action could be extracted by fitting the model to the data. The exposure rate dependence on the first mutation rate that has been detected for the joint fit of the EPIC data with either the CPS-II or the British doctors’ data (Table VI) is clearly associated with these two historic sets of data. These joint fits are at the 5% significance level statistically worse descriptions than the separate fits, indicated by positive values for \( \Delta \text{corr} \) in Table VI. The joint fit of EPIC males and British doctors’ data was, however, only slightly worse than the separate fits.

The British doctors’ data had previously been analysed (24,70). Moolgavkar et al. (70) found that with these data it was not possible to distinguish among various hypotheses regarding the relative roles of the two mutation rates and the kinetics of intermediate cell growth in cigarette smoke-induced lung cancer. In their study, however, an approximate solution of the two-mutation model was applied. In a later analysis the exact solution was used and it was found that cigarette smoking affected the first mutation rate and the kinetics of intermediate cell division but not the second mutation rate (12).

The results of the present study demonstrate that the simplest model description of the EPIC data did not allow for any smoking rate dependence in the first mutation rate. For the exposure rate dependencies of the second mutation rate and the rate of net clonal expansion a saturating behaviour was found. When the TSCE model was applied to the EPIC data, the results found for the biological action of cigarette smoke in lung carcinogenesis were consistent with the findings of the group at RIVM. This includes the strong similarities found in the risk patterns.

Earlier analyses that also used the two-stage model but other data sets came to different conclusions. Little et al. (14), for example, tested two- and three-mutation models on a case-control and on a cohort data set of lung cancer mortality in the Colorado Plateau uranium miners. They found that the first mutation rate was dependent on cigarette-smoke exposure in accordance with the findings of Luebeck et al. (71). In addition, the latter group also found a strong effect of cigarette smoke on the proliferation rate of initiated cells (71). It should, however, be mentioned that these earlier studies involved individuals with significant radiation exposure. The modelling presented here shows that for the EPIC data it is difficult to separate effects of smoking on different stages but that more information on effects on the first mutation rate could be found when studies are done with early starters—early stoppers. In the EPIC study the follow-up time may be too short to make a conclusive inference about the smoking influence on the different stages that are involved in carcinogenesis. Therefore, public health implications also should be considered with caution at the present stage.

From the abundance of scientific studies conducted on the biological effects caused by cigarette smoke, it is evident that both mutational and promoting effects can be induced. This reflects the findings of the present study.

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**References**


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